

24.33. Model: A confined particle can have only discrete values of energy.

Solve: (a) Equation 24.14 simplifies to

$$E_n = \frac{h^2}{8mL^2} n^2 = \frac{(6.63 \times 10^{-34} \text{ Js})^2}{8(9.11 \times 10^{-31} \text{ kg})(0.70 \times 10^{-9} \text{ m})^2} = (1.231 \times 10^{-19} \text{ J})n^2$$

Thus, $E_1 = (1.231 \times 10^{-19} \text{ J})(1^2) = 1.23 \times 10^{-19} \text{ J}$, $E_2 = (1.231 \times 10^{-19} \text{ J})(2^2) = 4.92 \times 10^{-19} \text{ J}$, and $E_3 = 1.11 \times 10^{-18} \text{ J}$.

(b) The energy is $E_2 - E_1 = 4.92 \times 10^{-19} \text{ J} - 1.23 \times 10^{-19} \text{ J} = 3.69 \times 10^{-19} \text{ J}$.

(c) Because energy is conserved, the photon will carry an energy of $E_2 - E_1 = 3.69 \times 10^{-19} \text{ J}$. That is,

$$E_2 - E_1 = E_{\text{photon}} = hf = \frac{hc}{\lambda} \Rightarrow \lambda = \frac{hc}{E_2 - E_1} = \frac{(6.63 \times 10^{-34} \text{ Js})(3.0 \times 10^8 \text{ m/s})}{3.69 \times 10^{-19} \text{ J}} = 539 \text{ nm}$$